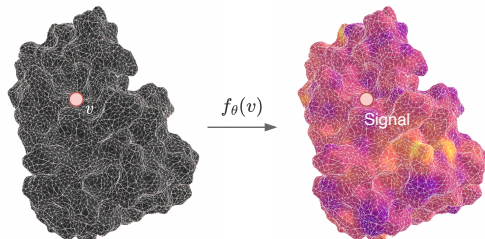


# Generalised Implicit Neural Representations

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Daniele Grattarola, Pierre Vandergheynst  
Neural Information Processing Systems 2022

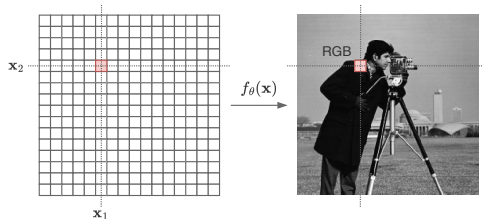


# Implicit neural representations

Given a signal or field  $f: \mathbb{R}^d \rightarrow \mathbb{R}^p$

Sample a regular grid  $\mathbf{y}_i = f(\mathbf{x}_i)$

Train neural network  $f_\theta: \mathbf{x}_i \mapsto \mathbf{y}_i$

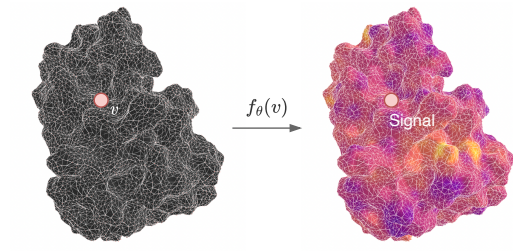


# Generalised implicit neural representations [1]

Given a signal or field  $f: \mathcal{T} \rightarrow \mathbb{R}^p$

Sample a graph signal  $\mathbf{y}_i = f(v_i)$

Train neural network  $f_\theta: v_i \mapsto \mathbf{y}_i$



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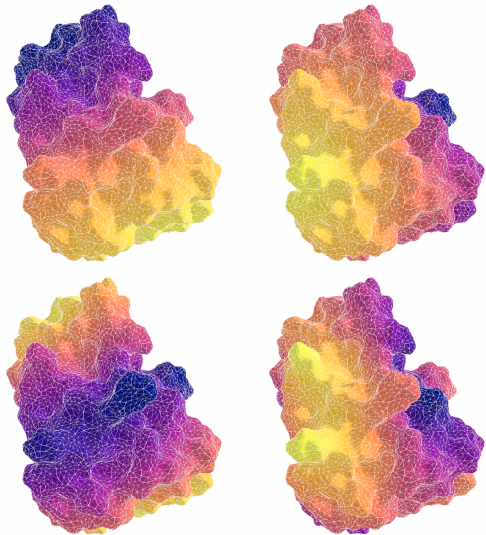
[1] D. Grattarola et al., "Generalised implicit neural representations," *Advances in Neural Information Processing Systems*, 2022.

# Generalised implicit neural representations [1]

Use spectral positional encodings as coordinates:

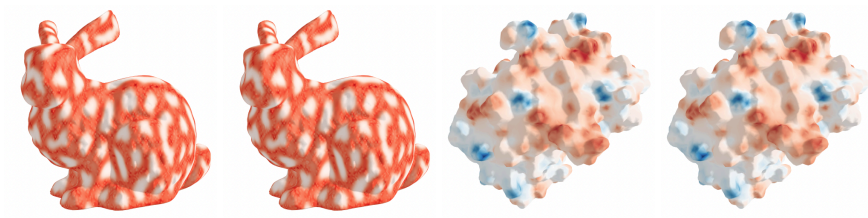
$$\mathbf{e}_i = \sqrt{n} \underbrace{[\mathbf{u}_{1,i}, \dots, \mathbf{u}_{k,i}]^T}_{\text{Laplacian eigenvectors}} \in \mathbb{R}^k$$

LB eigenfunctions for  $n \rightarrow \infty$ .





# Experiments

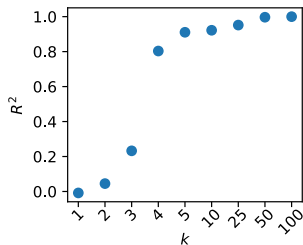


Ground truth signals vs. signals predicted by the GINR.

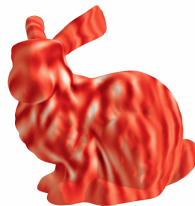
	Bunny	Protein	US Election
$R^2$	1.000	1.000	0.999
MSE	$9.14 \cdot 10^{-8}$	$1.17 \cdot 10^{-10}$	$1.45 \cdot 10^{-3}$

Approximation error

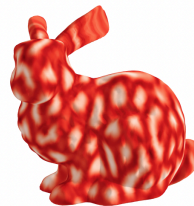
## Experiments - Size of embeddings



(a)  $k = 2$



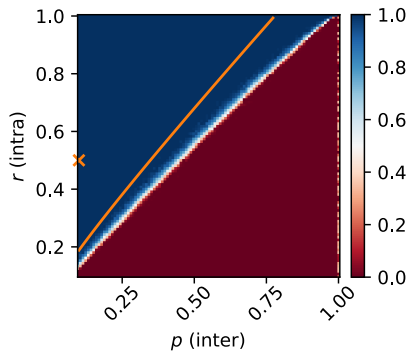
(b)  $k = 3$



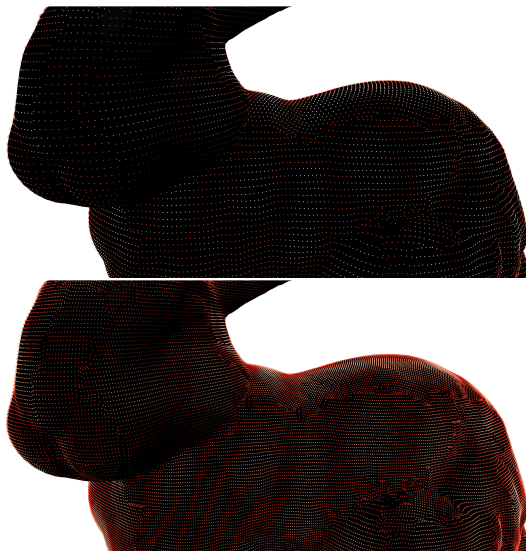
(c)  $k = 4$

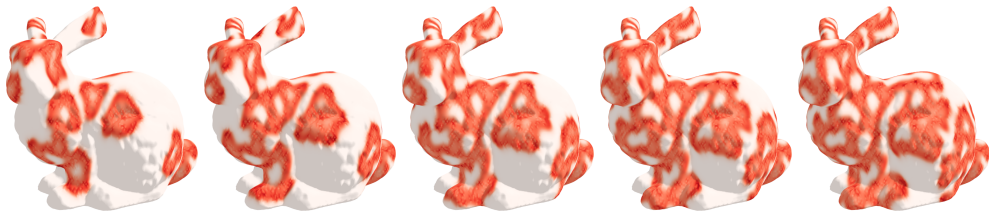
**Left:**  $R^2$  vs.  $k$ ; **Right:** signals learned by the INR for  $k = 2, 3, 4$ .

# Experiments - Transferability



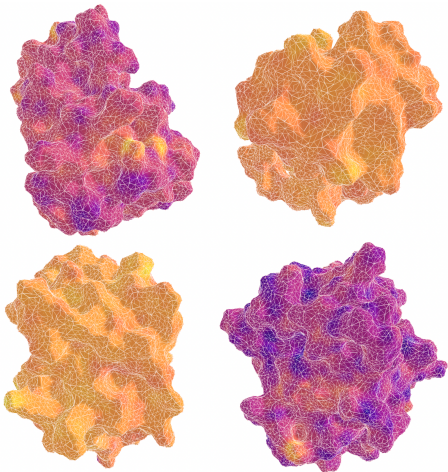
Toy problem with SBM.



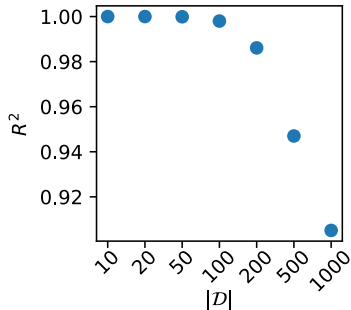


Signals predicted by the conditional GINR  $f_{\theta}(\mathbf{e}_i, t)$

## Experiments - Conditional GINRs



$f_{\theta}(\mathbf{e}_i, \mathbf{z}_d)$  for node  $i$  and protein  $d$ .

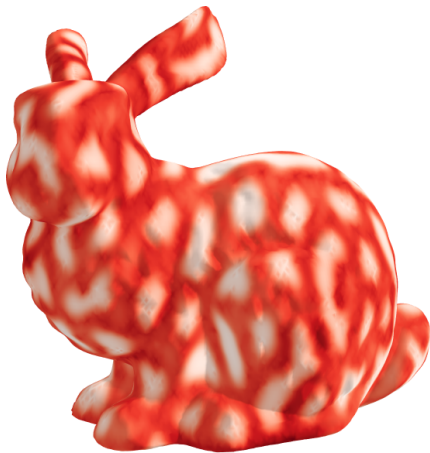


Good performance up to 100s of proteins.

## Experiments - Solving differential equations



(a) Laplacian (supervision,  $\Delta f_\theta$ )

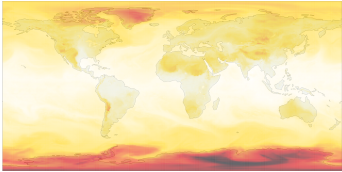


(b) Reconstructed ( $f_\theta$ )

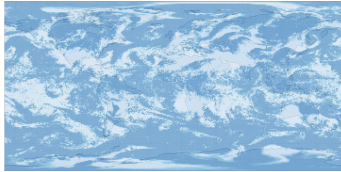


(c) Original ( $f$ )

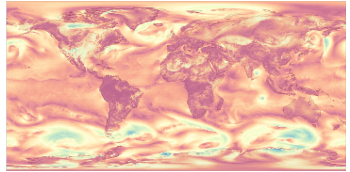
# Experiments - Weather modelling



(a) Temperature



(b) Clouds



(c) Wind



Data from the National Oceanic and Atmospheric Administration (NOAA).



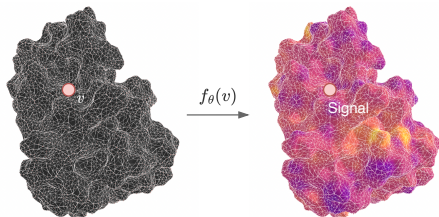
## Generalised Implicit Neural Representations

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Neural Information Processing Systems 2022

[github.com/danielegrattarola/GINR](https://github.com/danielegrattarola/GINR)

[arxiv.org/abs/2205.15674](https://arxiv.org/abs/2205.15674)



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- [1] D. Grattarola and P. Vandergheynst, “Generalised implicit neural representations,” *Advances in Neural Information Processing Systems*, 2022.